

Artificial Intelligence

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Learning Outcomes Knowledge based Agents

- Knowledge base (KB)
 - A set of sentences expressing in knowledge representation language
 - Represent some assertion about the world
- Knowledge-based Agent
 - Tell the knowledge base what it perceives
 - Ask the knowledge base what action is should perform
 - Tell the knowledge base which action was chosen
 - The agent executes the action
- Ask: query what is known
 - Forward chaining and backward chaining
- Tell: add new sentences to the knowledge base
 - Decision tree

Bayesian Theorem

$$P(A|B) = \frac{P(A \cap B)}{P(B)}.$$

$$P(B|A) = \frac{P(A \cap B)}{P(A)}.$$

$$P(A|B) P(B) = P(A \cap B) = P(B|A) P(A).$$

$$P(A|B) = \frac{P(B|A) P(A)}{P(B)}.$$

Bayes' Rule

$$\begin{array}{c} \text{posterior} \\ \curvearrowright \\ P(C | \mathbf{x}) = \frac{\overset{\text{prior}}{P(C)} \overset{\text{likelihood}}{p(\mathbf{x} | C)}}{\underset{\text{evidence}}{p(\mathbf{x})}} \end{array}$$

$$P(C = 0) + P(C = 1) = 1$$

$$p(\mathbf{x}) = p(\mathbf{x} | C = 1)P(C = 1) + p(\mathbf{x} | C = 0)P(C = 0)$$

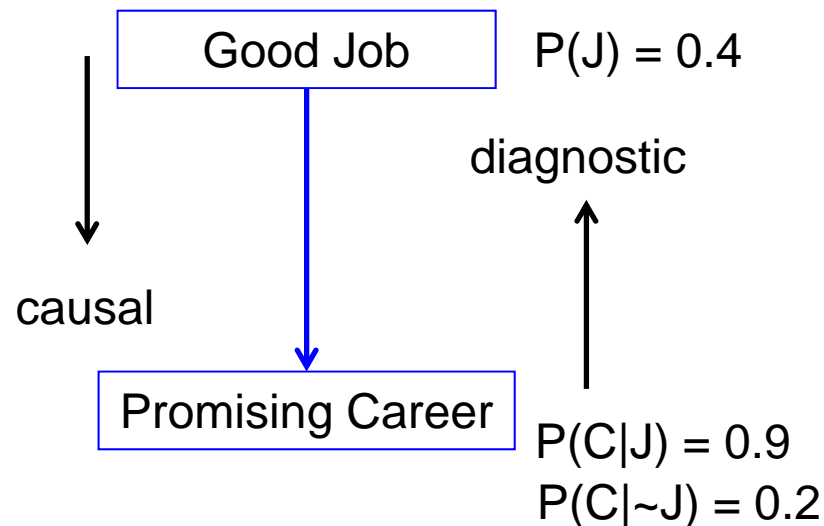
$$p(C = 0 | \mathbf{x}) + P(C = 1 | \mathbf{x}) = 1$$

Problem

- 40% students can get a good job when they appear as freshman in job market
 - 90% students have promising career path if the first job is good
 - 20% students have promising career path even if the first job is not good

Diagnostic Inference

- Diagnostic inference
 - Knowing promising career,
 - What is the probability that the good first job is the cause?

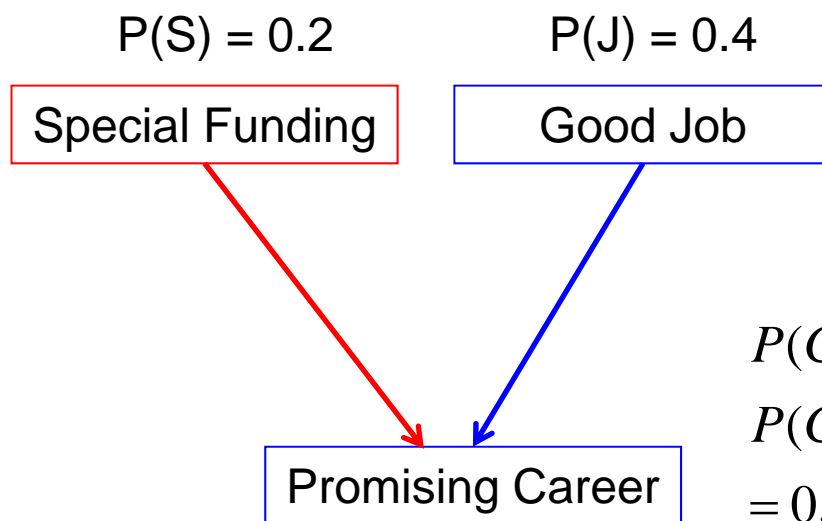


$$\begin{aligned} P(J | C) &= \frac{P(C | J) * P(J)}{P(C)} \\ &= \frac{0.9 * 0.4}{P(C | J) * P(J) + P(C | \sim J) * P(\sim J)} \\ &= \frac{0.36}{0.36 + 0.2 * (1 - 0.4)} \\ &= 0.75 \end{aligned}$$

Problem

- 40% students can get a good job when they appear as freshman in job market
 - 90% students have promising career path if the first job is good
 - 20% students have promising career path even if the first job is not good
- Government has 20% probability to set special funding for young person to startup
 - With both good job and special funding, 95% students have promising career path
 - Without good job and special funding, 10% students have promising career path
 - With good job and no special funding, 90% students have promising career path
 - Without good job but have special funding support, 90% students have promising career path

Causal vs Diagnostic Inference



- Causal inference
 - Knowing special funding,
 - What is the probability leading to promising career?

$$\begin{aligned} P(C | S) &= \\ &P(C | S, J)P(J | S) + P(C | S, \sim J)P(\sim J | S) \\ &= 0.95 * P(J) + 0.9 * P(\sim J) \end{aligned}$$

$$= 0.95 * 0.4 + 0.9 * 0.6$$

$$= 0.92$$

$$P(C|J,S) = 0.95$$

$$P(C|J,\sim S) = 0.9$$

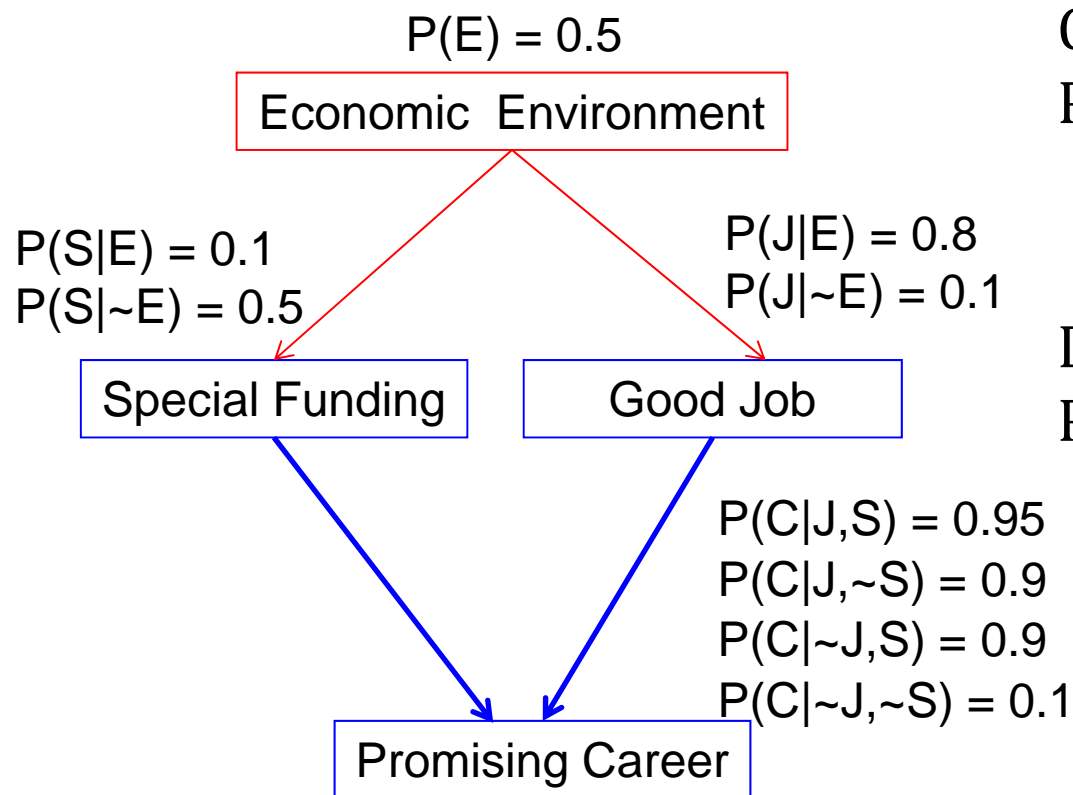
$$P(C|\sim J,S) = 0.9$$

$$P(C|\sim J,\sim S) = 0.1$$

Problem

- When the economic condition is good
 - 80% students can get a good job
 - Otherwise, 10% can get a good job
- When the economic condition is good
 - Government has 10% probability to set special funding for young person to startup
 - Otherwise 50% probability to set special funding for young person to startup
- The probability of good economic condition is 50%
- What is the probability of promising path when the economic environment is good
 - What is the probability of the economic environment is good when we observe the promising career path

Bayesian Networks



Causal inference
 $P(C|E) = 0.76$

Diagnostic inference
 $P(E|C) = 0.58$